

Math, Grade 5 (IMRA)

Subject: Mathematics

Grade: 05

Expectations: 46

Breakouts: 136

(a) Introduction.

1. The desire to achieve educational excellence is the driving force behind the Texas essential knowledge and skills for mathematics, guided by the college and career readiness standards. By embedding statistics, probability, and finance, while focusing on computational thinking, mathematical fluency, and solid understanding, Texas will lead the way in mathematics education and prepare all Texas students for the challenges they will face in the 21st century.
2. The process standards describe ways in which students are expected to engage in the content. The placement of the process standards at the beginning of the knowledge and skills listed for each grade and course is intentional. The process standards weave the other knowledge and skills together so that students may be successful problem solvers and use mathematics efficiently and effectively in daily life. The process standards are integrated at every grade level and course. When possible, students will apply mathematics to problems arising in everyday life, society, and the workplace. Students will use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution. Students will select appropriate tools such as real objects, manipulatives, algorithms, paper and pencil, and technology and techniques such as mental math, estimation, number sense, and generalization and abstraction to solve problems. Students will effectively communicate mathematical ideas, reasoning, and their implications using multiple representations such as symbols, diagrams, graphs, computer programs, and language. Students will use mathematical relationships to generate solutions and make connections and predictions. Students will analyze mathematical relationships to connect and communicate mathematical ideas. Students will display, explain, or justify mathematical ideas and arguments using precise mathematical language in written or oral communication.
3. For students to become fluent in mathematics, students must develop a robust sense of number. The National Research Council's report, "Adding It Up," defines procedural fluency as "skill in carrying out procedures flexibly, accurately, efficiently, and appropriately." As students develop procedural fluency, they must also realize that true problem solving may take time, effort, and perseverance. Students in Grade 5 are expected to perform their work without the use of calculators.
4. The primary focal areas in Grade 5 are solving problems involving all four operations with positive rational numbers, determining and generating formulas and solutions to expressions, and extending measurement to area and volume. These focal areas are supported throughout the mathematical strands of number and operations, algebraic reasoning, geometry and measurement, and data analysis. In Grades 3-5, the number set is limited to positive rational numbers. In number and operations, students will apply place value and identify part-to-whole relationships and equivalence. In algebraic reasoning, students will represent and solve problems with expressions and equations, build foundations of functions through patterning, identify prime and composite numbers, and use the order of operations. In geometry and measurement, students will classify two-dimensional figures, connect geometric attributes to the measures of three-dimensional figures, use units of measure, and represent location using a coordinate plane. In data analysis, students will represent and interpret data.
5. Statements that contain the word "including" reference content that must be mastered, while those containing the phrase "such as" are intended as possible illustrative examples.

(b) Knowledge and Skills Statements

- (1) Mathematical process standards. The student uses mathematical processes to acquire and demonstrate mathematical understanding. The student is expected to:
- (A) apply mathematics to problems arising in everyday life, society, and the workplace;
 - (i) apply mathematics to problems arising in everyday life
 - (ii) apply mathematics to problems arising in society
 - (iii) apply mathematics to problems arising in the workplace
 - (B) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process and the reasonableness of the solution;
 - (i) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the problem-solving process
 - (ii) use a problem-solving model that incorporates analyzing given information, formulating a plan or strategy, determining a solution, justifying the solution, and evaluating the reasonableness of the solution
 - (C) select tools, including real objects, manipulatives, paper and pencil, and technology as appropriate, and techniques, including mental math, estimation, and number sense as appropriate, to solve problems;
 - (i) select tools, including real objects as appropriate, to solve problems
 - (ii) select tools, including manipulatives as appropriate, to solve problems
 - (iii) select tools, including paper and pencil as appropriate, to solve problems
 - (iv) select tools, including technology as appropriate, to solve problems
 - (v) select techniques, including mental math as appropriate, to solve problems
 - (vi) select techniques, including estimation as appropriate, to solve problems
 - (vii) select techniques, including number sense as appropriate, to solve problems
 - (D) communicate mathematical ideas, reasoning, and their implications using multiple representations, including symbols, diagrams, graphs, and language as appropriate;
 - (i) communicate mathematical ideas using multiple representations, including symbols as appropriate
 - (ii) communicate mathematical ideas using multiple representations, including diagrams as appropriate
 - (iii) communicate mathematical ideas using multiple representations, including graphs as appropriate
 - (iv) communicate mathematical ideas using multiple representations, including language as appropriate
 - (v) communicate mathematical reasoning using multiple representations, including symbols as appropriate
 - (vi) communicate mathematical reasoning using multiple representations, including diagrams as appropriate
 - (vii) communicate mathematical reasoning using multiple representations, including graphs as appropriate
 - (viii) communicate mathematical reasoning using multiple representations, including language as appropriate
 - (ix) communicate [mathematical ideas'] implications using multiple representations, including symbols as appropriate
 - (x) communicate [mathematical ideas'] implications using multiple representations, including diagrams as appropriate

- (xi) communicate [mathematical ideas'] implications using multiple representations, including graphs as appropriate
- (xii) communicate [mathematical ideas'] implications using multiple representations, including language as appropriate
- (xiii) communicate [mathematical reasoning's] implications using multiple representations, including symbols as appropriate
- (xiv) communicate [mathematical reasoning's] implications using multiple representations, including diagrams as appropriate
- (xv) communicate [mathematical reasoning's] implications using multiple representations, including graphs as appropriate
- (xvi) communicate [mathematical reasoning's] implications using multiple representations, including language as appropriate

(E) create and use representations to organize, record, and communicate mathematical ideas;

- (i) create representations to organize mathematical ideas
- (ii) use representations to organize mathematical ideas
- (iii) create representations to record mathematical ideas
- (iv) use representations to record mathematical ideas
- (v) create representations to communicate mathematical ideas
- (vi) use representations to communicate mathematical ideas

(F) analyze mathematical relationships to connect and communicate mathematical ideas; and

- (i) analyze mathematical relationships to connect mathematical ideas
- (ii) analyze mathematical relationships to communicate mathematical ideas

(G) display, explain, and justify mathematical ideas and arguments using precise mathematical language in written or oral communication.

- (i) display mathematical ideas using precise mathematical language in written or oral communication
- (ii) display mathematical arguments using precise mathematical language in written or oral communication
- (iii) explain mathematical ideas using precise mathematical language in written or oral communication
- (iv) explain mathematical arguments using precise mathematical language in written or oral communication
- (v) justify mathematical ideas using precise mathematical language in written or oral communication
- (vi) justify mathematical arguments using precise mathematical language in written or oral communication

(2) Number and operations. The student applies mathematical process standards to represent, compare, and order positive rational numbers and understand relationships as related to place value. The student is expected to:

(A) represent the value of the digit in decimals through the thousandths using expanded notation and numerals;

- (i) represent the value of the digit in decimals through the thousandths using expanded notation
- (ii) represent the value of the digit in decimals through the thousandths using numerals

(B) compare and order two decimals to thousandths and represent comparisons using the symbols $>$, $<$, or $=$

- (i) compare two decimals to thousandths
 - (ii) order two decimals to thousandths
 - (iii) represent comparisons using the symbols $>$, $<$, or $=$
- (C) round decimals to tenths or hundredths.
- (i) round decimals to tenths or hundredths
- (3) Number and operations. The student applies mathematical process standards to develop and use strategies and methods for positive rational number computations in order to solve problems with efficiency and accuracy. The student is expected to:
- (A) estimate to determine solutions to mathematical and real-world problems involving addition, subtraction, multiplication, or division;
- (i) estimate to determine solutions to mathematical problems involving addition, subtraction, multiplication, or division
 - (ii) estimate to determine solutions to real-world problems involving addition, subtraction, multiplication, or division
- (B) multiply with fluency a three-digit number by a two-digit number using the standard algorithm;
- (i) multiply with fluency a three-digit number by a two-digit number using the standard algorithm
- (C) solve with proficiency for quotients of up to a four-digit dividend by a two-digit divisor using strategies and the standard algorithm;
- (i) solve with proficiency for quotients of up to a four-digit dividend by a two-digit divisor using strategies
 - (ii) solve with proficiency for quotients of up to a four-digit dividend by a two-digit divisor using the standard algorithm
- (D) represent multiplication of decimals with products to the hundredths using objects and pictorial models, including area models;
- (i) represent multiplication of decimals with products to the hundredths using objects
 - (ii) represent multiplication of decimals with products to the hundredths using pictorial models, including area models
- (E) solve for products of decimals to the hundredths, including situations involving money, using strategies based on place-value understandings, properties of operations, and the relationship to the multiplication of whole numbers;
- (i) solve for products of decimals to the hundredths, including situations involving money, using strategies based on place-value understandings
 - (ii) solve for products of decimals to the hundredths, including situations involving money, using properties of operations
 - (iii) solve for products of decimals to the hundredths, including situations involving money, using the relationship to the multiplication of whole numbers
- (F) represent quotients of decimals to the hundredths, up to four-digit dividends and two-digit whole number divisors, using objects and pictorial models, including area models;
- (i) represent quotients of decimals to the hundredths, up to four-digit dividends and two-digit whole number divisors, using objects

- (ii) represent quotients of decimals to the hundredths, up to four-digit dividends and two-digit whole number divisors, using pictorial models, including area models
- (G) solve for quotients of decimals to the hundredths, up to four-digit dividends and two-digit whole number divisors, using strategies and algorithms, including the standard algorithm;
- (i) solve for quotients of decimals to the hundredths, up to four-digit dividends and two-digit whole number divisors, using strategies
 - (ii) solve for quotients of decimals to the hundredths, up to four-digit dividends and two-digit whole number divisors, using algorithms, including the standard algorithm
- (H) represent and solve addition and subtraction of fractions with unequal denominators referring to the same whole using objects and pictorial models and properties of operations;
- (i) represent addition of fractions with unequal denominators referring to the same whole using objects
 - (ii) represent addition of fractions with unequal denominators referring to the same whole using pictorial models
 - (iii) represent addition of fractions with unequal denominators referring to the same whole using properties of operations
 - (iv) represent subtraction of fractions with unequal denominators referring to the same whole using objects
 - (v) represent subtraction of fractions with unequal denominators referring to the same whole using pictorial models
 - (vi) represent subtraction of fractions with unequal denominators referring to the same whole using properties of operations
 - (vii) solve addition of fractions with unequal denominators referring to the same whole using objects
 - (viii) solve addition of fractions with unequal denominators referring to the same whole using pictorial models
 - (ix) solve addition of fractions with unequal denominators referring to the same whole using properties of operations
 - (x) solve subtraction of fractions with unequal denominators referring to the same whole using objects
 - (xi) solve subtraction of fractions with unequal denominators referring to the same whole using pictorial models
 - (xii) solve subtraction of fractions with unequal denominators referring to the same whole using properties of operations
- (I) represent and solve multiplication of a whole number and a fraction that refers to the same whole using objects and pictorial models, including area models;
- (i) represent multiplication of a whole number and a fraction that refers to the same whole using objects
 - (ii) represent multiplication of a whole number and a fraction that refers to the same whole using pictorial models, including area models
 - (iii) solve multiplication of a whole number and a fraction that refers to the same whole using objects
 - (iv) solve multiplication of a whole number and a fraction that refers to the same whole using pictorial models, including area models
- (J) represent division of a unit fraction by a whole number and the division of a whole number by a unit fraction such as $1/3 \div 7$ and $7 \div 1/3$ using objects and pictorial models, including area models

- (i) represent division of a unit fraction by a whole number using objects
 - (ii) represent division of a unit fraction by a whole number using pictorial models, including area models
 - (iii) represent division of a whole number by a unit fraction using objects
 - (iv) represent division of a whole number by a unit fraction using pictorial models, including area models
- (K) add and subtract positive rational numbers fluently; and
- (i) add positive rational numbers fluently
 - (ii) subtract positive rational numbers fluently
- (L) divide whole numbers by unit fractions and unit fractions by whole numbers.
- (i) divide whole numbers by unit fractions
 - (ii) divide unit fractions by whole numbers
- (4) Algebraic reasoning. The student applies mathematical process standards to develop concepts of expressions and equations. The student is expected to:
- (A) identify prime and composite numbers;
- (i) identify prime numbers
 - (ii) identify composite numbers
- (B) represent and solve multi-step problems involving the four operations with whole numbers using equations with a letter standing for the unknown quantity;
- (i) represent multi-step problems involving the four operations with whole numbers using equations with a letter standing for the unknown quantity
 - (ii) solve multi-step problems involving the four operations with whole numbers using equations with a letter standing for the unknown quantity
- (C) generate a numerical pattern when given a rule in the form $y = ax$ or $y = x + a$ and graph;
- (i) generate a numerical pattern when given a rule in the form $y = ax$ or $y = x + a$
 - (ii) graph [the numerical pattern]
- (D) recognize the difference between additive and multiplicative numerical patterns given in a table or graph;
- (i) recognize the difference between additive and multiplicative numerical patterns given in a table or graph
- (E) describe the meaning of parentheses and brackets in a numeric expression;
- (i) describe the meaning of parentheses in a numeric expression
 - (ii) describe the meaning of brackets in a numeric expression
- (F) simplify numerical expressions that do not involve exponents, including up to two levels of grouping;
- (i) simplify numerical expressions that do not involve exponents, including up to two levels of grouping
- (G) use concrete objects and pictorial models to develop the formulas for the volume of a rectangular prism, including the special form for a cube ($V = l \times w \times h$, $V = s \times s \times s$, and $V = Bh$); and
- (i) use concrete objects to develop the formulas for the volume of a rectangular prism, including the special form for a cube ($V = l \times w \times h$, $V = s \times s \times s$, and $V = Bh$)

- (ii) use pictorial models to develop the formulas for the volume of a rectangular prism, including the special form for a cube ($V = l \times w \times h$, $V = s \times s \times s$, and $V = Bh$)
- (H) represent and solve problems related to perimeter and/or area and related to volume.
 - (i) represent problems related to perimeter and/or area
 - (ii) represent problems related to volume
 - (iii) solve problems related to perimeter and/or area
 - (iv) solve problems related to volume
- (5) Geometry and measurement. The student applies mathematical process standards to classify two-dimensional figures by attributes and properties. The student is expected to:
 - (A) classify two-dimensional figures in a hierarchy of sets and subsets using graphic organizers based on their attributes and properties
 - (i) classify two-dimensional figures in a hierarchy of sets and subsets using graphic organizers based on their attributes
 - (ii) classify two-dimensional figures in a hierarchy of sets and subsets using graphic organizers based on their properties
- (6) Geometry and measurement. The student applies mathematical process standards to understand, recognize, and quantify volume. The student is expected to:
 - (A) recognize a cube with side length of one unit as a unit cube having one cubic unit of volume and the volume of a three-dimensional figure as the number of unit cubes (n cubic units) needed to fill it with no gaps or overlaps if possible; and
 - (i) recognize a cube with side length of one unit as a unit cube having one cubic unit of volume
 - (ii) recognize the volume of a three-dimensional figure as the number of unit cubes (n cubic units) needed to fill it with no gaps or overlaps if possible
 - (B) determine the volume of a rectangular prism with whole number side lengths in problems related to the number of layers times the number of unit cubes in the area of the base.
 - (i) determine the volume of a rectangular prism with whole number side lengths in problems related to the number of layers times the number of unit cubes in the area of the base
- (7) Geometry and measurement. The student applies mathematical process standards to select appropriate units, strategies, and tools to solve problems involving measurement. The student is expected to:
 - (A) solve problems by calculating conversions within a measurement system, customary or metric
 - (i) solve problems by calculating conversions within a measurement system, customary or metric
- (8) Geometry and measurement. The student applies mathematical process standards to identify locations on a coordinate plane. The student is expected to:
 - (A) describe the key attributes of the coordinate plane, including perpendicular number lines (axes) where the intersection (origin) of the two lines coincides with zero on each number line and the given point $(0, 0)$; the x -coordinate, the first number in an ordered pair, indicates movement parallel to the x -axis starting at the origin; and the y -coordinate, the second number, indicates movement parallel to the y -axis starting at the origin
 - (i) describe the key attributes of the coordinate plane, including perpendicular number lines (axes) where the intersection (origin) of the two lines coincides with zero on each number line and the given point $(0,0)$

- (ii) describe the key attributes of the coordinate plane, including the x-coordinate, the first number in an ordered pair, indicates movement parallel to the x-axis starting at the origin
 - (iii) describe the key attributes of the coordinate plane, including the y-coordinate, the second number, indicates movement parallel to the y-axis starting at the origin
- (B) describe the process for graphing ordered pairs of numbers in the first quadrant of the coordinate plane; and
- (i) describe the process for graphing ordered pairs of numbers in the first quadrant of the coordinate plane
- (C) graph in the first quadrant of the coordinate plane ordered pairs of numbers arising from mathematical and real-world problems, including those generated by number patterns or found in an input-output table.
- (i) graph in the first quadrant of the coordinate plane ordered pairs of numbers arising from mathematical problems, including those generated by number patterns or found in an input-output table
 - (ii) graph in the first quadrant of the coordinate plane ordered pairs of numbers arising from real-world problems, including those generated by number patterns or found in an input-output table
- (9) Data analysis. The student applies mathematical process standards to solve problems by collecting, organizing, displaying, and interpreting data. The student is expected to:
- (A) represent categorical data with bar graphs or frequency tables and numerical data, including data sets of measurements in fractions or decimals, with dot plots or stem-and-leaf plots;
- (i) represent categorical data with bar graphs or frequency tables
 - (ii) represent numerical data, including data sets of measurements in fractions or decimals, with dot plots or stem-and-leaf plots
- (B) represent discrete paired data on a scatterplot; and
- (i) represent discrete paired data on a scatterplot
- (C) solve one- and two-step problems using data from a frequency table, dot plot, bar graph, stem-and-leaf plot, or scatterplot.
- (i) solve one-step problems using data from a frequency table, dot plot, bar graph, stem-and-leaf plot, or scatterplot
 - (ii) solve two-step problems using data from a frequency table, dot plot, bar graph, stem-and-leaf plot, or scatterplot
- (10) Personal financial literacy. The student applies mathematical process standards to manage one's financial resources effectively for lifetime financial security. The student is expected to:
- (A) define income tax, payroll tax, sales tax, and property tax;
- (i) define income tax
 - (ii) define payroll tax
 - (iii) define sales tax
 - (iv) define property tax
- (B) explain the difference between gross income and net income;
- (i) explain the difference between gross income and net income
- (C) identify the advantages and disadvantages of different methods of payment, including check, credit card, debit card, and electronic payments;

- (i) identify the advantages of different methods of payment, including check payments
 - (ii) identify the advantages of different methods of payment, including credit card payments
 - (iii) identify the advantages of different methods of payment, including debit card payments
 - (iv) identify the advantages of different methods of payment, including electronic payments
 - (v) identify the disadvantages of different methods of payment, including check payments
 - (vi) identify the disadvantages of different methods of payment, including credit card payments
 - (vii) identify the disadvantages of different methods of payment, including debit card payments
 - (viii) identify the disadvantages of different methods of payment, including electronic payments
- (D) develop a system for keeping and using financial records;
- (i) develop a system for keeping financial records
 - (ii) develop a system for using financial records
- (E) describe actions that might be taken to balance a budget when expenses exceed income; and
- (i) describe actions that might be taken to balance a budget when expenses exceed income
- (F) balance a simple budget.
- (i) balance a simple budget